

Bio390

Problem: Solubility (SOLUTIONS)

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1. Calculate how much oxygen will dissolve in one liter of fresh water at sea level (i.e., $P_b = 760$ mm Hg). Assume the air is saturated with water vapor (look in notes), the temperature is 20°C , and oxygen constitutes 20.94% of the volume in of the dry fraction of the air. The solubility coefficient for oxygen in water at 20°C is about $31 \text{ mlO}_2 / (\text{liter H}_2\text{O} * \text{atm})$

From the notes: $P_{\text{H}_2\text{O}}$ at 20°C when saturated = 17.5 torr.

Recall that O_2 and other gases (except water vapor) are always given as either F or % on a dry gas basis. Therefore

$$P_{\text{O}_2} = (P_b - P_{\text{H}_2\text{O}}) * \% \text{O}_2 / 100 = (760 - 18) \text{ torr} * 20.94 / 100 = 742 \text{ torr} * 0.2094$$

$$P_{\text{O}_2} = 155 \text{ torr}$$

At equilibrium, the amount of O_2 that will be dissolved (D_{O_2}) is:

$$D_{\text{O}_2} = \alpha_{\text{O}_2} * P_{\text{O}_2} = 31 \text{ ml O}_2 / (\text{liter H}_2\text{O} * \text{atm}) * 155 \text{ torr} * 1 \text{ atm} / 760 \text{ torr}$$

$$D_{\text{O}_2} = 31 \text{ ml O}_2 / (\text{liter H}_2\text{O} * \text{atm}) * 0.2039 \text{ atm}$$

$D_{\text{O}_2} = 6.3 \text{ ml O}_2 / \text{liter of water.}$

Note that this corresponds to 0.6 ml O_2 per dl (100 ml) of water; a set of units we will more commonly use when we discuss blood gas transport. Actually, since in mammals the blood is typically between 36 and 39°C , the amount of O_2 carried in solution is only about half that (around $3 \text{ ml O}_2 / \text{dl plasma}$)

2. Calculate how much oxygen will dissolve in one liter of fresh water at an altitude where the barometric pressure is 450 mm Hg. Again assume the air is saturated with water vapor, the temperature is 20° , and oxygen constitutes 20.94% of the volume in air on a dry gas basis.

Just like before except that the pressure is 450 torr.

$$P_{\text{O}_2} = (P_b - P_{\text{H}_2\text{O}}) * \% \text{O}_2 / 100 = (450 - 18 \text{ torr}) * 0.2094 = 432 * 0.2094 = 90 \text{ torr}$$

$$D_{\text{O}_2} = \alpha_{\text{O}_2} * P_{\text{O}_2} = 31 \text{ ml O}_2 / (\text{liter H}_2\text{O} * \text{atm}) * 90 \text{ torr} * 1 \text{ atm} / 760 \text{ torr}$$

= $3.7 \text{ ml O}_2 / \text{liter H}_2\text{O}$