

Oxygen Transport by the Blood -- SOLUTION

Given the following:

For an HCT = 40 **bound** O_2 at saturation = 20 ml/dl

P_{aO_2} = 100 torr

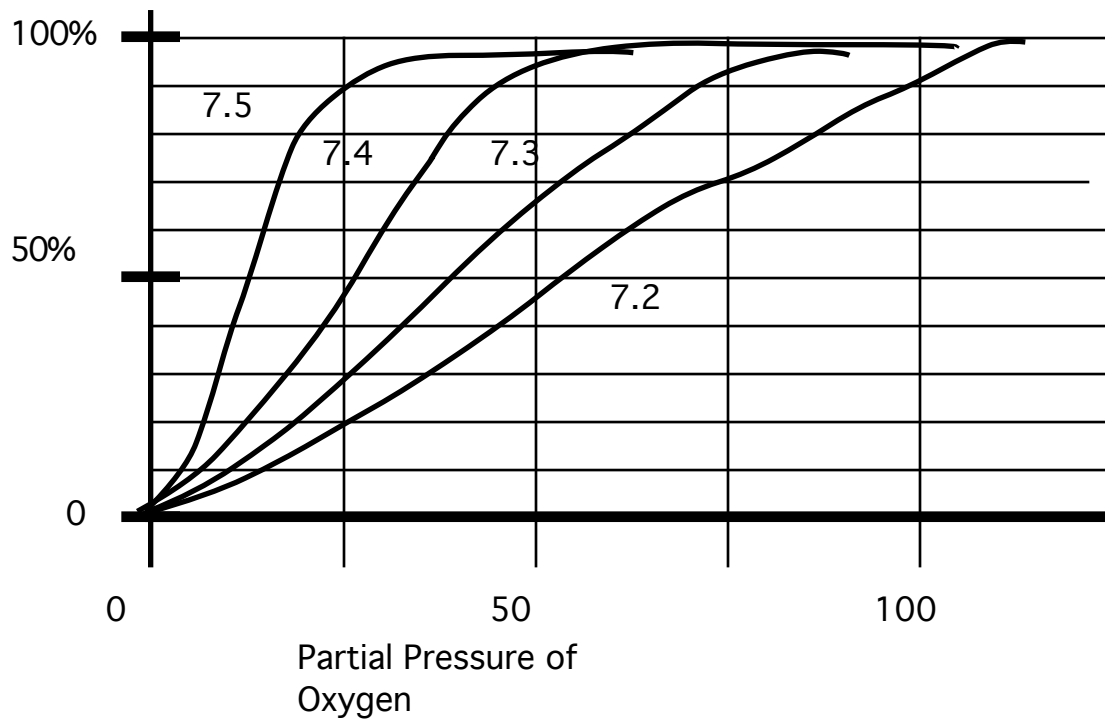
P_{vO_2} = 25 torr

Solubility of O_2 = 0.01 ml O_2 /torr * dl blood

HCT = 50

arterial pH = 7.4

RA pH = 7.2



(a) Find the oxygen content of arterial blood.

From the graph, simply go from the P_{aO_2} which in this case is 100 up to the arterial blood curve, here the pH = 7.4 curve. The blood is saturated. Now we need the O_2 carrying capacity of this person's blood. Since their hct = 50%, then their blood can carry $50/40 * 20 \text{ ml } O_2 / \text{ dl blood} = 25 \text{ ml } O_2 / \text{ dl blood}$ bound to Hb when the blood is saturated (which it is).

But there is also dissolved O_2 – the amount is simply the P_{O_2} times the solubility, so $100 \text{ torr} * 0.01 \text{ mL } O_2 / (\text{dL} * \text{torr}) = 1 \text{ mL } O_2$

Thus: $25 + 1 = 26 \text{ mL } O_2 / \text{dL}$

(b) Find the total oxygen content of mixed venous (RA) blood. Why is RA blood termed "mixed venous"?

Same method as before except $P_{aO_2} = 25 \text{ torr}$ and the $pH = 7.2$. Using the graph, this gives a % sat of 20%. Thus, the amount of O_2 carried is:

$$20/100 * 25 \text{ ml } O_2 / \text{dl blood} = 5 \text{ ml } O_2 / \text{dl blood}$$

Likewise, the amount in solution is

$$25 \text{ torr} * 0.01 \text{ mL } O_2 / (\text{dL} * \text{torr}) = 0.25 \text{ mL } O_2 / \text{dL}$$

and the total in the RA is bound plus dissolved
= $5.25 \text{ mL } O_2 / \text{dL}$

(c) Find the total AV (arterial to venous) difference in oxygen content in ml O_2 per 100 ml blood.

This is the difference between the results in (a) and (b) which is the difference in bound O_2 plus the difference in the dissolved O_2 (see (e) below).

$$\Delta \text{ Dissolved } O_2 = \alpha (P_{aO_2} - P_{vO_2}) = 0.01 \text{ mL } O_2 / \text{torr} * \text{dl blood} * (100 - 25 \text{ torr}) = 0.75 \text{ mL } O_2 / \text{dl blood}$$

$$\Delta \text{ bound } O_2 = 25 - 5 \text{ mL } O_2 / \text{dl} = 20 \text{ mL } O_2 / \text{dl}$$

Thus, A-V O_2 is $20 + 0.75 \text{ mL } O_2 / \text{dl} = \mathbf{20.75 \text{ mL } O_2 / \text{dl}}$

**OR using the numbers in (a) and (b) it is the A-V (i.e., RA) difference in O₂ content
= 26.00-5.25 =20.75 mL O₂ / dL**

(d) Compare the value you found for (c) with what would have happened in the absence of a Bohr effect -- *i.e.*, if there had been no change in affinity due to a decrease in pH.

The Δ Dissolved O₂ will be the same as the example, as will be the arterial bound O₂. However, if there is no Bohr effect we will continue to use the pH = 7.4 graph to get the % sat of venous blood at 25 torr. This value is about 45%. Thus,

$$\Delta \text{ Bound O}_2 = 25 \text{ ml O}_2 / \text{dl blood} * (100 - 45)/100 = 13.75 \text{ ml O}_2 / \text{dl blood}$$

which is $13.75 / 20.75 = 0.66$ as much O₂ as was delivered from bound as with the Bohr effect.

Total O₂ delivered in this case is:

$$\Delta \text{ Bound} + \Delta \text{ Dissolved} = 13.75 + 0.75 = \mathbf{14.5 \text{ ml O}_2 / \text{dl blood}}$$

which is $14.5 / 20.75 * 100 = \mathbf{70\%}$ of what was delivered with the Bohr effect.

(e) Write a general mathematical expression that would allow you to solve for AV difference in oxygen content using the variables you used in parts (a) to (d) above.

$$\text{O}_2 \text{ delivered} = \Delta \text{ Bound O}_2 + \Delta \text{ Dissolved O}_2$$

$$= \text{O}_2 \text{ capacity} * (\% \text{SAT arterial} - \% \text{SAT venous})/100 + \alpha (P_{aO_2} - P_{vO_2})$$

(f) Assume that the person lost 50% of her/his ability to carry oxygen bound to hemoglobin. If the person still needs the same amount of O₂ to live, what would happen to the following (make qualitative predictions (up, down, no change) only).

(i) A-V saturation: increase this difference, probably by decreasing decreasing venous % saturation (removal of more O₂ from blood in tissues) while maintaining P_{aO₂}. Lactic

acid production would hopefully not be a major "aid" in unloading bound O_2 .

(ii) A-V Dissolved O_2 : As above, decrease PvO_2 – note again that this will also result in a decrease in venous % saturation – the change in P_{vO_2} would precede any change in % venous saturation.

(iii) Cardiac Output: Increase cardiac output -- delivery of more volume of blood per time could easily compensate for the reduced amount of O_2 available in each volume of blood that is delivered.

(iv) Anything else?: intervention -- breathe gas with a high P_{O_2} .