

RESPIRATION CALCULATIONSⁱ

Assume the values given below were obtained from measurements made on a healthy human at sea level.

$$F_{ECO_2}: 0.037$$

$$F_{IO_2}: 0.2094$$

$$F_{ACO_2}: 0.054$$

$$F_{ICO_2}: 0.00$$

$$F_{EO_2}: 0.1737$$

$$F_{AO_2}: 0.1557$$

$$P_{(total)}: 760 \text{ mm Hg}$$

$$pK_a \text{ (carbonic acid bicarb system)}: 6.10$$

$$P_{AH_2O}: 47 \text{ mm}$$

$$\text{Systemic arterial plasma pH}: 7.40$$

$$\dot{V}_E: \frac{6 \text{ liters}}{\text{min}}$$

$$\alpha_{CO_2}: \frac{0.03 \text{ mM}}{\text{L} \cdot \text{mmHg}}$$

$$R: 0.85$$

$$f: \frac{12 \text{ breaths}}{\text{min}}$$

ESTIMATE:

(a) \dot{V}_{CO_2}

$$\dot{V}_{CO_2} = F_{ECO_2} * \dot{V}_E = 0.037 * 6 \text{ l/min} = 222 \text{ ml / min}$$

$$\dot{V}_{O_2}$$

(b) $\dot{V}_{O_2} = (F_{IO_2} - F_{EO_2}) / (1 - F_{EO_2}) * \dot{V}_E$

$$= (0.2094 - 0.1737) / (1 - 0.1737) * 6 \text{ L/m} = 259 \text{ ml/min}$$

$$\dot{V}_A$$

ⁱ thanks to Dr. J.F. Anderson, Dept Zoology, Univ of Florida, Gainesville for the original idea for this problem

$$\text{(c) } \dot{V}_A = \dot{V}_{\text{CO}_2} / F_{\text{ACO}_2} = 0.2220 / 0.054 = 4.07 \text{ L / min}$$

(d) \dot{V}_D -- need \dot{V}_A from previous question

$$\dot{V}_D = \dot{V}_E - \dot{V}_A$$

$$= 6 \text{ L/ min} - 4.07 \text{ L/ min} = 1.93 \text{ L/ min}$$

(e) \dot{V}_D -- need \dot{V}_E from previous question

$$\dot{V}_D = \dot{V}_D / f = 1.93/12 = 0.160 \text{ L}$$

P_{ACO2}

$$(f) P_{ACO2} = F_{ACO2} * (P_b - P_{H2O}) = 0.054 * (760 - 47)$$

$$= 38.5 \text{ torr}$$

(g) systemic arterial $[HCO_3^-]$

The $P_{ACO2} = P_{aCO2}$, using H-H and given data:

$$[HCO_3^-] = \alpha_{P_{CO2}} * (\text{antilog}(pH - pKa))$$

$$= \frac{0.03 \text{ mmols}}{\text{L} \cdot \text{mm Hg}} * 38.5 * (10^{(7.4-6.1)})$$

$$[HCO_3^-] = 23 \text{ mM}$$

(h) P_{AO2}

$$P_{AO2} = F_{ACO2} * (P_b - P_{H2O}) = 0.1557 * (760 - 47)$$

= 111 torr

(i) P_{AN_2} We need to get this by subtraction since we have no value for $F_{A_{O_2}}$ but we do have values for $P_{A_{H_2O}}$, $P_{A_{O_2}}$ and $P_{a_{CO_2}}$ and total pressure.

$$P_{AN_2} = 760 - 111 (P_{A_{O_2}}) - 38.5 (P_{a_{CO_2}}) - 47 (P_{H_2O}) = 563 \text{ torr}$$

(j) F_{ACO_2} IF \dot{V}_A doubles and \dot{V}_{CO_2} stays the same as above

Recall that:

$$\dot{V}_A = \dot{V}_{CO_2} / F_{ACO_2}$$

or

$$F_{ACO_2} = \dot{V}_{CO_2} / \dot{V}_A$$

So, if \dot{V}_{CO_2} remains constant and \dot{V}_A doubles, then the F_{ACO_2} **will be cut in half**

(k) F_{ACO_2} IF breathing frequency doubles but \dot{V}_E and \dot{V}_{CO_2} stay the same as above

This one is easy. It appears that even though the subject is breathing at a higher rate, nevertheless, no hyperventilation is occurring since \dot{V}_E has not increased. However, the possibility that hypoventilation has occurred is still there (the person could be breathing faster and not ventilating their alveolar space sufficiently). However, since \dot{V}_{CO_2} remains the same we can be relatively (but not absolutely) certain that alveolar

ventilation is normal. Thus, **the most logical conclusion is that alveolar ventilation has remained the same.**

F_{ACO_2} IF both \dot{V}_A and \dot{V}_{CO_2} double

Recall from two problems previously:

$$F_{ACO_2} = \dot{V}_{CO_2} / \dot{V}_A$$

(I) If both double, there will be no change (F_{ACO_2} remains the same) since both change by the same amount.